ECE 488 – Automatic Control

Basics and Plant Modeling

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Compulsory Course in Electronic and Communication Engineering
Credits (3/0/3)

Course Webpage: http://ECE488.cankaya.edu.tr

Content and Structure

Content

- Modeling Dynamic Systems
- Linear State Space and Transfer Function Models
- Model Analysis
- Basic Control Concepts
- Control Loop Analysis
- Control Loop Design
- Matlab/Simulink Examples

Structure

- 3 lecture hours: Thursday 15:40 – 17:30; Friday 13:40
- Office hours: Friday 12:40 - 13:30

Grading and Literature

Grading

- 10 Quizzes (10%)
- 12 Homeworks (25%)
- 1 Midterm Exam (25%)
- 1 Final Exam (40 %)

Literature

- Goodwin, Graham, Graebe Stefan, Salgado, Mario: "Control System Design", Prentice-Hall, Inc., 2001 (ISBN: 0-13-958653-9) (Main Textbook)
- Ogata, Katsuhiko: "Modern Control Engineering (5th Edition)", Prentice-Hall, Inc., 2009 (ISBN: 0-13-615673-8)
- Astrom, Karl and Murray, Richard: "Feedback Systems: An Introduction for Scientists and Engineers", Princeton University Press, 2008 (ISBN: 0-691-13576-2)

Motivation: Basics

Control

Control is a discipline that is concerned with the automatic manipulation of a dynamic system's behavior

Dynamic System

System that shows dynamic dependency between input and output signals

- Signal is a time-varying physical quantity (e.g. position, velocity, temperature, voltage, current, . . .)
- Usually, dynamic systems possess memory
- Dynamic systems are for example modeled by differential equations, difference equations, transfer functions

Motivation: Dynamic System in Control

Detailed Graphical Representation

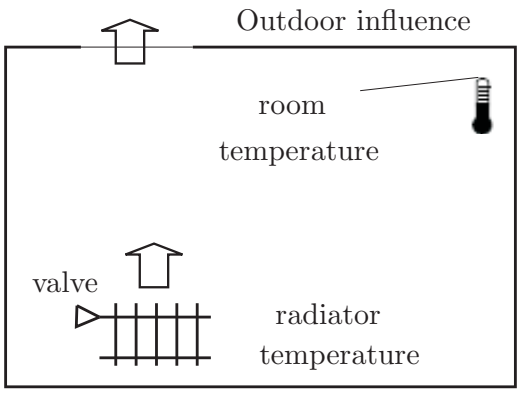
Gap 1

Manipulation of a Dynamic System

Application of appropriate inputs such that the system state/output behaves as desired even in the presence of disturbances

Examples: Room Temperature System

Schematic



Graphical Representation

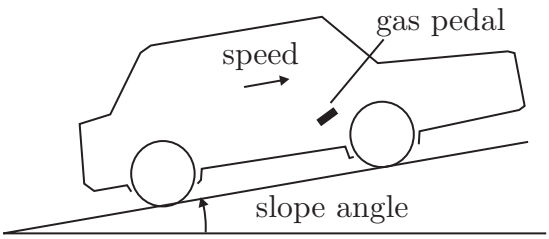
Gap 2

Control Task

- Desired (specified) behavior: keep room temperature constant
- Manipulation: automatically adjust valve position

Examples: Vehicle Speed

Schematic



Graphical Representation

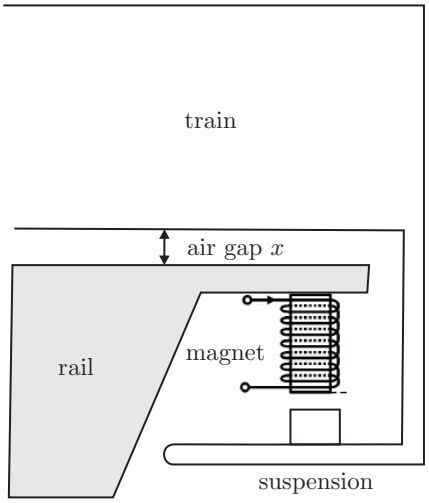
Gap 3

Control Task

- Desired (specified) behavior: keep vehicle speed constant
- Manipulation: automatically adjust pedal position

Examples: Magnetic Suspension

Schematic



Graphical Representation

Gap 4

Control Task

- Desired (specified) behavior: Move to/keep specified position
- Manipulation: automatically adjust current in the coil

Examples: Movies

Inverted Pendulum

- Desired (specified) behavior: Keep pendulum upright
- Manipulation: horizontally move cart

  $\Rightarrow$ http://www.rt.eei.uni-erlangen.de/FGnls/video/inverted_pendulum.wmv

Automatic Parking

- Desired (specified) behavior: Reach parking position (without collision)
- Manipulation: automatically adjust speed and steering angle

  $\Rightarrow$ http://www.rt.eei.uni-erlangen.de/FGnls/video/automatic_parking.wmv

Ball on Plate

- Desired (specified) behavior: follow path/keep position
- Manipulation: automatically change orientation of plate

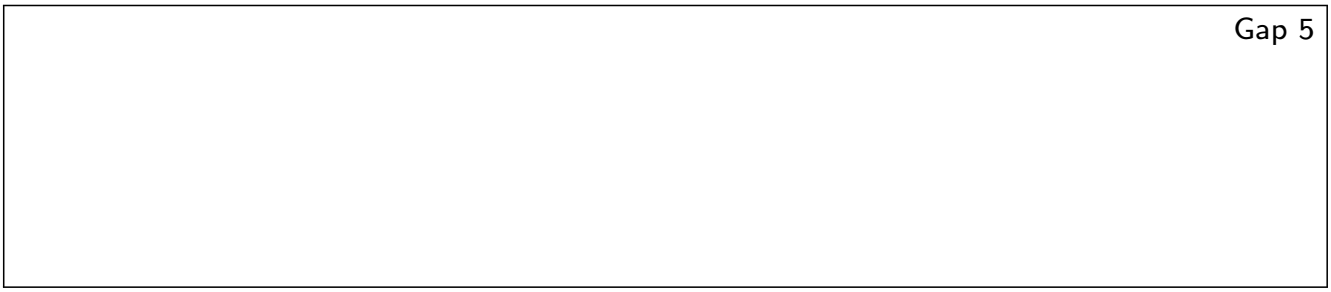
  $\Rightarrow$ http://www.rt.eei.uni-erlangen.de/FGnls/video/ball_on_plate.wmv

Control Engineering: Basic Task

Main Task of Control Engineering

Design and realize technical appliance – controller – that enforces the desired output behavior of the plant when connected to the plant

Feedforward Control



$\Rightarrow$ Feedforward controller provides appropriate input such that the plant follows a given reference signal

Control Engineering: Basic Principles

Feedback Control

Gap 6

⇒ Feedback controller tries to compensate the difference between a reference signal and the measured output signal

Remarks

- Control problems occur in many subject areas
- Examples: process engineering, electrical engineering, communication networks, automotive applications, medicine, chemistry, biology, . . .
  ⇒ Mathematical abstraction of control problems to enable interdisciplinary application

Control Engineering: General Solution Procedure

Procedure

1. Mathematical modeling of plant
   ⇒ Abstraction from the physical problem
2. Analysis of the plant behavior
   ⇒ Determine basic properties of the plant and their implications on the design
3. Controller design
   ⇒ Achieve desired plant behavior
4. Simulation and test on the real system
   ⇒ Verify if design goals are achieved

The main subjects of this lecture are items 1 to 3 for systems with a single input signal and a single output signal (SISO)

Plant Modeling: Basic Idea

A plant model is a mathematical description of the cause-effect relationship between the plant signals that are relevant for the design task

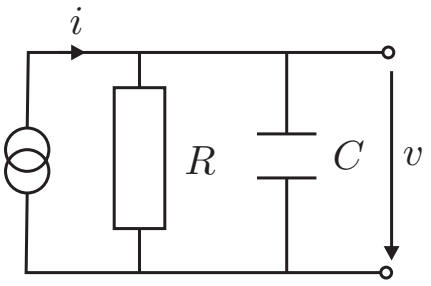
Remarks

- Different design tasks for the same system can lead to different plant models
- We focus on models for control tasks
- We consider as relevant signals
  - Input signals (signals that we can directly influence)
  - Output signals (signals that we want to manipulate)
  - Disturbance signals (signals that cannot be directly influenced and that can have a negative effect on the system)

Plant Modeling: Example

RC-Circuit

Gap 7



- Input: $u = i$
- Output: $y = v$

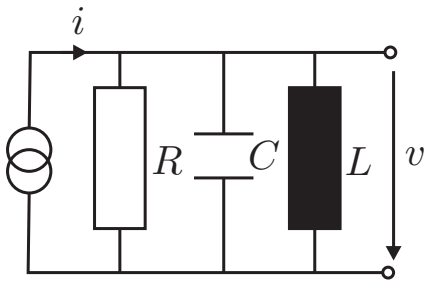
Differential Equation

$$C \cdot \frac{dy}{dt} + \frac{1}{R} \cdot y = u$$

Plant Modeling: Example

RLC-Circuit

Gap 8



- Input: $u = i$
- Output: $y = v$

Differential Equation

$$C \cdot \frac{d^2y}{dt^2} + \frac{1}{R} \cdot \frac{dy}{dt} + \frac{1}{L} \cdot y = \frac{du}{dt}$$

Plant Modeling: Basic Dynamic Behavior in this Lecture

Linear Time-invariant Ordinary Differential Equation (LTI ODE)

$$a_n y^{(n)} + a_{n-1} y^{(n-1)} + \cdots + a_1 \dot{y} + a_0 y = b_m u^{(m)} + b_{m-1} u^{(m-1)} + \cdots + b_1 \dot{u} + b_0 u$$

Notation

- y: output signal (in the time domain)
- u: input signal (in the time domain)
- $y^{(i)}$ ($u^{(i)}$): i-th time derivative of y (u)
- a_i, b_i: coefficients in $\mathbb{R}$
- n: highest derivative of y
- m: highest derivative of u

Block Diagram: Description

Characteristics of the Block Diagram

A block diagram is a graphical representation of the cause-effect relationship between signals by blocks and directed lines

⇒ Visualization of direction of action and interdependencies

Block Diagram Components

- Directed Lines: System signals and their direction of action
- Circles: Summation of signals

Gap 9

Block Diagram: Description

Gap 10

Block Diagram Components

- Rectangles: Dynamic relationship between signals: unique mapping from input signal to output signal

Gap 11

⇒ Rectangles and circles are transfer blocks

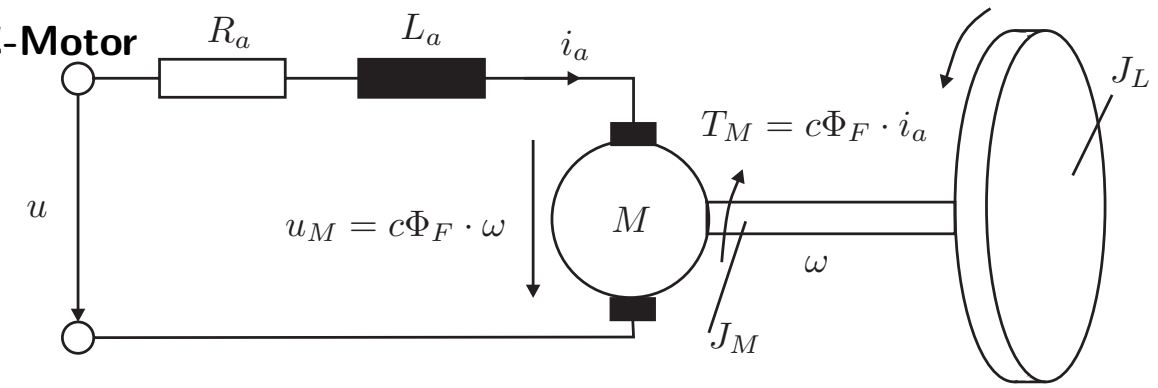
Block Diagram: Examples

RLC-Circuit

Gap 12

Plant Modeling: Example

DC-Motor



Variables

- u, i: input voltage, current
- u_M: induced voltage
- ω: rotational velocity
- T_M: motor torque

Parameters

- R_a: resistance
- L_a: inductance
- $c\Phi_F$: motor constant
- J_a: moment of inertia

Plant Modeling: System Equations

Computation

Gap 13

Plant Modeling: Block Diagram

Graphical Representation

Gap 14